

Solving Inequalities

Solve each inequality and graph its solution.

1)  $0 > 3x - 3 - 6$   $x < 3$

test a point:  $0$  for  $x$   
 $0 > 3(0) - 3 - 6$   
 $0 > -9$  true!  
 so shade toward  $0$ .

find boundary point:  $0 = 3x - 9$   
 $+9$   $+9$   
 $9 = 3x$   
 $\frac{9}{3} = \frac{3x}{3}$   $x = 3$  does not include 3 (so open circle).

3)  $-1 \leq 2n + 4 - 5$

$x \geq 0$

5)  $0 \leq 2n + 3n$

$x \geq 0$

7)  $7 < -(k-3) + 2$

$x > 2$

9)  $-5(1-4a) > -5$

$x > 0$

2)  $4x + 1 - 1 \geq -8$   $x \geq -2$

test a point on either side in inequality  
 I like 0!  
 $4(0) + 1 - 1 \geq -8$   
 $0 + 0 \geq -8$   
 $0 \geq -8$  true!  $0$  is a solution!  
 Shade!

$4x + 1 - 1 = -8$   
 $4x + 0 = -8$   
 $\frac{4x}{4} = \frac{-8}{4}$   
 $x = -2$   
 boundary pt.

4)  $-6 > 5n + 5 + 4$   $x < -3$

test a point on either side  
 I like 0!  
 $-6 > 5(0) + 9$   
 $-6 > 9$  not true!  
 Shade other side. not side that includes 0!

$-6 = 5n + 9$   
 $-9$   $-9$   
 $-15 = 5n$   
 $\frac{-15}{5} = \frac{5n}{5}$   
 $-3 = n$  ← boundary point.

6)  $2p - 4p \leq -2$   $x \geq 1$

test a point on either side.  
 I like 0!  
 $-2p \leq -2$   
 $-2(0) \leq -2$   
 $0 \leq -2$  not true!  
 Shade other side.

$2p - 4p = -2$   
 $-2p = -2$   
 $\frac{-2p}{-2} = \frac{-2}{-2}$   
 $p = 1$  ← boundary point.

8)  $3 - 2(n-4) > -1$   $x < 6$

test a point on either side.  
 Let's try 7!  
 $3 - 2(7-4) > -1$   
 $3 - 2(3) > -1$   
 $3 - 6 > -1$   
 $-3 > -1$  not true!  
 Shade other side!!

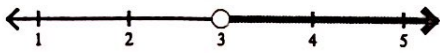
$3 - 2(n-4) = -1$   
 $-2n = -11$   
 $\frac{-2n}{-2} = \frac{-11}{-2}$   
 $n = 6$  ← boundary point.

10)  $-2(b+1) + 4 < 10$   $x > -4$

Let's use 0! My favorite!  
 $-2(0+1) + 4 < 10$   
 $-2(1) + 4 < 10$   
 $2 + 4 < 10$   
 $2 < 10$  true!  
 Shade the side that includes 0!

$-2(b+1) + 4 = 10$   
 $-2b - 2 + 4 = 10$   
 $-2b + 2 = 10$   
 $-2$   $-2$   
 $-2b = 8$   
 $\frac{-2b}{-2} = \frac{8}{-2}$   
 $b = -4$  ← boundary point.

$$11) a - 15 > -4(-6 + 3a)$$



$$X > 3$$

$$12) 3(6b - 1) > 18 - 3b$$



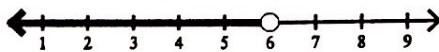
$$X > 1$$

$$13) 26 + m \geq 5(-6 + 3m)$$



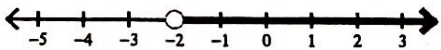
$$X \leq 4$$

$$14) 20 - 2p > -2(p + 2) + 4p$$



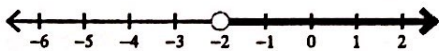
$$X < 6$$

$$15) x + 1 + 1 + 6x > 3(x - 4) - (x - 4)$$



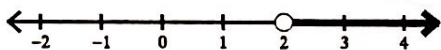
$$X > -2$$

$$16) -6(1 + 6x) < 6(1 - 5x)$$



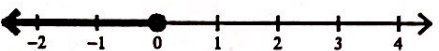
$$X > -2$$

$$17) 2(1 - 4r) < -2(r + 3) - 4$$



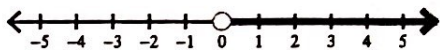
$$X > 2$$

$$18) -6(1 + 2x) \geq 6(2x - 1) + 2x$$



$$X \leq 0$$

$$19) -2(1 - 5x) > -(x + 1) - 1$$



$$X > 0$$

$$20) 5x - (x + 2) > -5(1 + x) + 3$$



$$X > 0$$

### Critical thinking questions:

21) Write an inequality with  $x$  on both sides whose solution is  $x \geq 2$

Many answers. Ex:  $2x \geq x + 2$

22) Name one particular solution to question #20.

Any number greater than zero. Ex: 4.7